

Towards the Improvement of Cuckoo Search Algorithm

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Abstract—Cuckoo search algorithm via Lévy flights by Xin-She Yang and Saush Deb [1] for optimizing a nonlinear function uses generation of random numbers with symmetric Lévy distribution obtained by Mantegna's algorithm. However, instead of using the original algorithm, its simplified version is used to generate Lévy flights during the Cuckoo Search algorithm [2]. A paper by Matteo Leccardi [3] describes three algorithms, namely, Mantegna's algorithm, rejection algorithm and McCulloch's algorithm to generate such random numbers and claims that McCulloch's algorithm outperforms the other two. The idea in this paper is to compare the performance of Mantegna's algorithm, its simplified version, and McCulloch's algorithm when each of them is incorporated in Cuckoo search algorithm to generate Lévy flights [4]. Moreover, a term similar to the Local Best component of PSO is added in updating the population while implementing the CS algorithm using simplified version of Mantegna's algorithm and the results are analyzed. Some other implementation oriented changes are also incorporated and their effect is studied.

Keywords-Cuckoo search, Lévy flights, Optimization, Random number generation, Mantegna's algorithm, McCulloch's algorithm, Modified Cuckoo Search Algorithm.

I. Introduction

During last few years, many nature inspired evolutionary algorithms have been developed for optimization. These algorithms work on the basis of random search in some suitable search region depending on the problem. Though it is a random search, it is not truly random because there is a mechanism in the algorithm which guides the search in such a manner that the solution vector gets improved step by step. Two crucial characteristics of these modern meta-heuristics are intensification (exploitation) and diversification (exploration). Intensification intends to search around the current best solutions, while diversification tries to explore the search space efficiently so that the algorithm does not get stuck into local optimum. Such algorithms have become quite popular and helping due to their efficiency in terms of robustness, accuracy, speed and simple implementation. But at the same time, they have some drawbacks like, one particular algorithm may be efficient for a specific class of optimization problems but may

not be so efficient for some other class of optimization problems or sometimes they get stuck into local optimum.

One of such nature inspired algorithms is Cuckoo Search algorithm (CS). The algorithm was developed by Xin-She Yang and Saush Deb in 2009 [1]. It was inspired by obligate brood parasitism of some cuckoo species by laying their eggs in to the nest of host birds. Those female parasitic cuckoos can imitate the colors and pattern of the eggs of the host species. So there are fewer chances that the host bird may identify and destroy the eggs. But, by chance, if the host bird discovers that the eggs are different, it will either destroy the eggs or may destroy the nest completely and build a new nest at different place. The timing of egg-laying of some species is also amazing. The parasitic cuckoo often chooses a host nest where the eggs are just laid. In general, the cuckoo eggs are hatched little earlier than the host eggs. As soon as the first cuckoo chick is hatched, it starts throwing out the host eggs blindly out of the nest so that it can increase the share of its food provided by the host bird.

The animals search for food in random manner. Their search path is made up of step by step random walk or flight which is based on the current location and the transition probability to the next location. Various studies show that the flight behavior of animals or birds has typical characteristics of Lévy flight. Lévy flight is a random walk where the step size is distributed according to the heavy tailed distribution. After a large number of steps, the distance from the origin of the flight tends to a stable distribution.

The CS algorithm has been modified by involving the information exchange between top eggs, or the best solutions, a concept similar to elitism in GA [5]. Its modified version is also hybridized with Conjugate Gradient Method to train Multi-Layer Perceptrons in [6]. It is applied for optimum design of spaces trusses [7] and for the selection of optimal machining parameters in milling operations [8]. The fact that, if a cuckoo's egg is very similar to a host's egg then it is less likely to be discovered, is used to modify the random walk in the algorithm in somewhat biased way [9]. It is also improved by varying its parameters relative to the generation number

[10] and it is applied to train feedforward neural networks to classify the iris and breast cancer data sets [11]. A new search strategy based on orthogonal learning strategy to enhance the exploitation ability of the basic cuckoo search algorithm is presented in [12]. Orthogonal design is used to produce all possible combinations of levels for a complete factorial experiment. The basic idea of orthogonal design is to utilize the properties of the fractional experiment for the efficient determination of the best combination of levels. Experimental results by the CS algorithm with this new search strategy are concluded as better than or at least comparable with the existing quality results. The algorithmic concepts of the CS, PSO, DE and ABC algorithms have been analyzed in [13]. The empirical results in this paper reveal that the problem solving CS algorithm is close to DE algorithm and the CS and DE algorithms supply more robust and precise results than the PSO and ABC algorithms.

Various applications of cuckoo search algorithm and some other optimization algorithms are presented by many researchers. In [14] an attempt is made to develop an artificial neural network (ANN) based model for CO₂ laser cutting of stainless steel. The laser cutting experiment is planned and conducted according to Taguchi's L₂₇ orthogonal array considering the four laser cutting parameters namely laser power, cutting speed, assist gas pressure and focus position. In order to obtain minimum surface roughness, the cutting parameters are optimized by integrating the ANN model with the Cuckoo Search algorithm. In one another application optimization of ATM cash is investigated using Genetic Algorithm [15]. Stocking cash in ATMs entails costs that can be broadly divided into two contributions, one financial cost and other operational costs. The financial cost is mainly due to the unused stock rated by annual passive interests. The operational costs are mainly due to time to perform and supervise the task, maintenance, out of service and risk of robbery. Therefore it is desirable to perform an efficient refill of ATMs so that the daily amount of stocked money can be minimized but same time assuring good cash dispensing service. Based on surveys, some important factors are taken into consideration and GA is implemented to optimize the cash in ATMs. A comparative study of performance of three algorithms GA, PSO and CS in clustering problems is done in [16]. Also, it is observed that under given set of parameters the CS algorithm works efficiently for majority of data sets under consideration and Lévy flights plays an important role. The main version of cuckoo search algorithm has been utilized to solve many connected problems. Moreover, a discrete binary CS algorithm has been developed and implemented efficiently on knapsack 0-1 problems as in [17]. An extensive comparative study of performance of the CS algorithm using some standard test functions, newly designed stochastic test functions and the constrained design optimization problems like welded beam design and spring design is done in [18] concluding far better results than the best results obtained by efficient PSO. Feature selection is an optimization technique used in face recognition technology. Feature selection removes the irrelevant, noisy and redundant data thus leading to the more accurate recognition of the face from the data base. Observing that the results of CS algorithm are better than PSO and ACO, a proposal of

applying the CS algorithm for feature selection is presented in [19].

In order to generate random numbers with symmetric Lévy distribution, some algorithms like Mantegna's algorithm, rejection algorithm and McCulloch's algorithm exist [3, 20]. The performance of these algorithms for Lévy noise generation has been compared in [3]. It shows that McCulloch's algorithm outperforms the other two. The natural question arises is that how the performance of Cuckoo Search algorithm is affected if McCulloch's Algorithm is used to generate the Lévy flight instead of Mantegna's algorithm. Moreover, it is also interesting to check the effect of adding a term similar to Local Best in PSO algorithm while generating the cuckoo population. Thoroughly examining the implementation of the CS algorithm [21], some other implementation oriented changes have become apparent for the possible betterment of the algorithm.

In this paper, we have implemented the Cuckoo Search algorithm with Mantegna's algorithm, the simplified version of Mantegna's algorithm, and the McCulloch's algorithm, incorporated into it one by one to generate the Lévy flights. For each of these cases, the algorithm is implemented on ten benchmark problems A to J. Moreover, various changes have been made in the algorithm and extensive experiments are carried out to test them on the same benchmark problems. The outputs obtained are analyzed and tabulated [Table 1]. The algorithm is implemented in MATLAB.

The remainder of this paper is organized as follows. Section II describes the working of all the algorithms used in this work. A list of benchmark problems on which our testing of algorithm has focused is given in section III, followed by the implementation of the algorithm in section IV. The results obtained are discussed in section V. Sections VI and VII contain conclusion and future work respectively.

II. Working of the algorithms

The Cuckoo Search algorithm via Lévy flights, Mantegna's algorithm, its simplified version algorithm and McCulloch's algorithm are described in the text follows. Discussion of other implementation oriented modifications are also mentioned thereafter.

A. Cuckoo Search via Lévy flights

Cuckoo Search algorithm is inspired by obligate brood parasitism of some cuckoo species by laying their eggs in to the nest of host birds. Those female parasitic cuckoos can imitate the colors and pattern of the eggs of the host species. For simplicity, it is assumed that there is only one egg at a time in a nest. The available egg in the host nest represents an initial solution. An egg laid by a cuckoo is representing a new solution generated by the algorithm. The algorithm works on the basis of following three assumptions:

- A cuckoo chooses a nest randomly to lay the egg and at a time only one egg is laid by the cuckoo.
- The best nests with the high quality egg (solution) will carry over to the next generations.
- The total number of available host nests is fixed and the host bird can discover a cuckoo's egg with a probability, $P_a \in [0, 1]$. In this case, the host bird either destroys the egg or

destroys the nest completely and builds up a new nest somewhere else.

The third assumption can be approximated as a fraction P_a of the total n nests that are replaced by the new nests having a new random solution. When generating new solution $X^{(t+1)}$ for, say, a cuckoo i , a Lévy flight is performed as

$$X_i^{(t+1)} = X_i^{(t)} + \alpha \oplus \text{Lévy}(\lambda)$$

where $\alpha > 0$ is the step size which should be related to the scales of the problem of interests. In most cases, $\alpha = 1$ is used. This equation is stochastic equation for random walk. In general, a random walk is a Markov chain whose next location depends only on the current location and the transition probability. The product \oplus means entrywise multiplications. The Lévy flight essentially provides a random walk while the random step length is drawn from a Lévy distribution

$$\text{Lévy} \sim u = t^{-\lambda}, \quad (1 < \lambda \leq 3)$$

which has an infinite variance with an infinite mean. Here the steps essentially form a random walk process with a power law step length distribution with a heavy tail.

The algorithm can also be extended to more complicated cases where each nest contains multiple eggs (a set of solutions). The algorithm can be summarized as per the following pseudo code:

Begin

The objective function is $f(X)$, $X = (x_1, x_2, \dots, x_D)$.

Generate an initial population with n solution vectors namely X_i , $i = 1, 2, \dots, n$.

While ($t < \text{Max interactions}$) and (termination condition not achieved)

Generate a new solution vector X_{new} via Lévy flight and evaluate its fitness say F_{new} .

Randomly select a vector say X_j from the current population and compare the function values $f(X_j)$ and $f(X_{new})$.

If $f(X_{new}) < f(X_j)$, replace X_j by X_{new} .

A fraction of the P_a of the worse nests is abandoned and new nests are generated.

Keep the quality solutions and find the current best solution vector

End while

Post process and results

End

B. Mantegna's algorithm

Mantegna's algorithm [22] produces random numbers according to a symmetric Lévy stable distribution. It was developed by R. Mantegna. The algorithm needs the distribution parameters $\alpha \in [0.3, 1.99]$, $c > 0$, and the number of iterations, n . It also requires the number of points to be generated. When not specified, it generates only one point. If an input parameter will be outside the range, an error message will be displayed and the output contains an array of NaNs (Not a number). The algorithm is described in following steps:

$$v = \frac{x}{|y|^{\frac{1}{\alpha}}}$$

where x and y are normally distributed stochastic variables. But x is calculated as $x\sigma_x$, where

$$\sigma_x(\alpha) = \left[\frac{\Gamma(\alpha + 1) \sin\left(\frac{\pi\alpha}{2}\right)}{\Gamma\left(\frac{\alpha+1}{2}\right) \alpha 2^{\frac{(\alpha-1)}{2}}}\right]^{\frac{1}{\alpha}}, \quad \sigma_y = 1$$

The resulting distribution has the same behavior of a Lévy distribution for large values of random variable ($|v| \gg 0$).

Using the nonlinear transformation

$$w = \left\{ [K(\alpha) - 1] e^{\frac{-|v|}{C(\alpha)}} + 1 \right\} v,$$

the sum $z_{cn} = \frac{1}{n^{\frac{1}{\alpha}}} \sum_1^n w_k$ quickly converges to a Lévy stable distribution. The convergence is assured by central limit theorem. The value of $K(\alpha)$ can be obtained as

$$K(\alpha) = \frac{\alpha \Gamma\left(\frac{\alpha+1}{2}\right)}{\Gamma\left(\frac{1}{\alpha}\right)} \left[\frac{\alpha \Gamma\left(\frac{\alpha+1}{2}\right)}{\Gamma(\alpha + 1) \sin\left(\frac{\pi\alpha}{2}\right)} \right]^{\frac{1}{\alpha}}$$

Also, $C(\alpha)$ is the result of a polynomial fit to the values tabulated in [14], obtained by resolving the following integral equation:

$$\frac{1}{\pi \sigma_x} \int_0^\infty q^{\frac{1}{\alpha}} \exp\left[-\frac{q^2}{2} - \frac{\frac{2}{\alpha} C(\alpha)^2}{2\sigma_x^2}\right] dq = \frac{1}{\pi} \int_0^\infty \cos\left(\left(\frac{[K(\alpha) - 1]}{e} + 1\right) C(\alpha)\right) \exp(-q^\alpha) dq$$

The required random variable is given by $z = C^{\frac{1}{\alpha}} z_{cn}$.

C. Simplified version algorithm

Mantegna's algorithm uses two normally distributed stochastic random variables to generate a third random variable which has the same behavior of a Lévy distribution for large values of the random variable. Further it applies a nonlinear transformation to let it quickly converge to a Lévy stable distribution. However, the difference between the Mantegna's algorithm and its simplified version used by Xin-She Yang and Saush Deb as a part of cuckoo search algorithm is that the simplified version does not apply the aforesaid nonlinear transformation to generate Lévy flights. It uses the entry-wise multiplication of the random number so generated and distance between the current solution and the best solution obtained so far (which look similar to the Global best term in PSO) as a transition probability to move from the current location to the next location to generate a Markov chain of solution vectors. However, PSO also uses the concept of Local best. Implementation of the algorithm is very efficient with the use of Matlab's vector capability, which significantly reduces the running time. The algorithm starts with taking one by one solution from the initial population and then replacing it by a new vector generated using the steps described below.

$$\begin{aligned} \text{stepsize} &= 0.01 * v.* (s - \text{current best}) \\ \text{new}_{soln} &= \text{old}_{soln} + \text{stepsize}.* z \end{aligned}$$

where v is same as Mantegna's algorithm above with σ_x calculated for $\alpha = \frac{3}{2}$. z is again a normally distributed stochastic variable.

D. McCulloch's algorithm

The algorithm was developed by J. H. McCulloch. It is based on an explicit formula to generate random numbers from a Lévy process, as a function of two independent variables w and φ with uniform distribution in the range $(-\frac{\pi}{2}, \frac{\pi}{2})$ and standard exponential distribution, respectively is given by

$$c \frac{N_1 N_2}{D} + \tau$$

where

$$N_1 = \sin \left[\alpha \varphi + \tan^{-1} \left(\beta \tan(\alpha \pi / 2) \right) \right]$$

$$N_2 = \left(\cos \left[(1 - \alpha) \varphi - \tan^{-1} \left(\beta \tan(\alpha \pi / 2) \right) \right] \right)^{\frac{1}{\alpha} - 1}$$

$$D = \left(\cos \left[\tan^{-1} \left(\beta \tan(\alpha \pi / 2) \right) \right] \right)^{\frac{1}{\alpha}} (\cos \varphi)^{\frac{1}{\alpha} w^{\frac{1}{\alpha} - 1}}$$

It returns an $n \times m$ matrix of random numbers. The required parameters are characteristic exponent α , skewness parameter β , scale c , and location parameter τ . The minimum value of α is 0.1 because of the non-negligible possibility of overflow. When an input is not in the valid range, the resultant matrix contains NaNs. Here the symmetric case of $\beta = 0$ is considered. In this case, the algorithm uses the following formula:

$$x = c \left(\frac{\cos((1 - \alpha)\varphi)}{w} \right)^{\frac{1}{\alpha} - 1} \frac{\sin(\alpha\varphi)}{\cos(\varphi)^{\frac{1}{\alpha}}} + \tau$$

Two special cases are handled separately:

$\alpha = 2$ (Gaussian case). In this case,

$$x = c2\sqrt{w} \sin(\varphi) + \tau$$

$\alpha = 1$ (Cauchy case). In this case,

$$x = c \tan(\varphi) + \tau$$

E. Simplified version including P-best

In the simplified version algorithm, the concept of global best (G-best) is used in similar manner as in PSO algorithm. But it does not include the current best vector (P-best) used in PSO for generating the new solutions. We have included both the G-best and the P-best in the simplified version algorithm to generate the new solutions.

F. Simplified version including P-best and with $P_a < 0.25$

In generating the new nests (solution vectors), the code given in [21] modifies the 75% components of the total vectors in a generation, by considering the probability $P_a = 0.25$. We changed the probability P_a so that now only 25% components of total vectors in a generation are modified to form the new solutions. Other values of probability can also be tried for. Of course, the algorithm again includes the P-best.

G. Simplified version including P-best and modifying all components of 75% vectors

The simplified version algorithm changes 75% of the components of the total vectors in a generation to produce the new solutions. A vector represents a nest. If only some of the components of a vector are modified then it is not relevant to the actual philosophy of the algorithm which says that the entire nest is either being survived or destroyed as mentioned in the third assumption. So we made some changes in the algorithm which, rather than some components, actually

modifies all components of 75% of the vectors in a generation, leaving 25% unchanged.

H. Simplified version including P-best and modifying all components of 25% vectors

This variant is similar to algorithm G with the modification that all components of 25% of the vectors in a generation are changed to produce the new solutions.

III. Benchmark Problems

We have implemented the algorithms on the following benchmark problems, A to J [23, 24, 25].

A. Sphere function

$$f(X) = \sum_{i=1}^D (x_i - 1)^2$$

Search space: $x_i \in [-5, 5], i = 1, 2, \dots, D$

Global minimum: $\mathbf{0}$ at $(1, 1, \dots, 1)$

B. Ackley function

$$f(X) = -20 \exp \left\{ -0.2 \sqrt{\frac{1}{D} \sum_{i=1}^D x_i^2} \right\} - \exp \left\{ \frac{1}{D} \sum_{i=1}^D \cos(2\pi x_i) \right\} + 20 + e$$

Search space: $x_i \in [-5, 5], i = 1, 2, \dots, D$

Global minimum: $\mathbf{0}$ at $X = (0, 0, \dots, 0)$

C. Dixon and Price function

$$f(X) = (x_1 - 1)^2 + \sum_{i=2}^D i(2x_i^2 - x_{i-1})^2$$

Search space: $x_i \in [0, 2], i = 1, 2, \dots, D$

Global minimum: $\mathbf{0}$ at $X = (x_1, x_2, \dots, x_D)$

where, $x_i = 2^{-\left(\frac{2^i - 2}{2^i}\right)}, i = 1, 2, \dots, D$.

D. Griewank function

$$f(X) = \frac{1}{4000} \sum_{i=1}^D x_i^2 - \prod_{i=1}^D \cos\left(\frac{x_i}{\sqrt{i}}\right) + 1$$

Search space: $x_i \in [-5, 5], i = 1, 2, \dots, D$

Global minimum: $\mathbf{0}$ at $X = (0, 0, \dots, 0)$

E. Step function

$$f(X) = \sum_{i=1}^D |x_i + 0.5|$$

Search space: $x_i \in [-5, 5], i = 1, 2, \dots, D$

Global minimum: $\mathbf{0}$ at $X = (-0.5, -0.5, \dots, -0.5)$

F. Levy function

$$f(X) = \sin^2(\pi y_1) + \sum_{i=1}^{D-1} [(y_i - 1)^2 (1 + 10 \sin^2(\pi y_i + 1))] + (y_D - 1)^2 (1 + 10 \sin^2(2\pi y_D)),$$

where, $y_i = 1 + \frac{x_i - 1}{4}$, $i = 1, 2, \dots, D$

Search space: $x_i \in [-10, 10]$, $i = 1, 2, \dots, D$

Global minimum: $\mathbf{0}$ at $X = (1, 1, \dots, 1)$

G. Generalized Schwfel 2.6 function

$$f(X) = 418.9829D - \sum_{i=1}^D x_i \sin \sqrt{|x_i|}$$

Search space: $x_i \in [300, 500]$, $i = 1, 2, \dots, D$

Global minimum: $\mathbf{0}$ at $(420.9687, 420.9687, \dots, 420.9687)$

H. Generalized Rozenbrock function

$$f(X) = \sum_{i=1}^{D-1} [100(x_i^2 - x_{i+1})^2 + (x_i - 1)^2]$$

Search space: $x_i \in [-5, 5]$, $i = 1, 2, \dots, D$

Global minimum: $\mathbf{0}$ at $(1, 1, \dots, 1)$

I. Rastrigin function

$$f(X) = 10D + \sum_{i=1}^D [x_i^2 - 10 \cos(2\pi x_i)]$$

Search space: $x_i \in [-0.9, 0.9]$, $i = 1, 2, \dots, D$

Global minimum: $\mathbf{0}$ at $X = (0, 0, \dots, 0)$

J. Weierstrass function

$$f(X) = \sum_{i=1}^D \left\{ \sum_{k=0}^{k_{max}} [a^k \cos(2\pi b^k (x_i + 0.5))] \right\} - D \sum_{k=0}^{k_{max}} [a^k \cos(2\pi b^k 0.5)]$$

$a=0.5$, $b=3$, $k_{max}=20$.

Search space: $x_i \in [-0.5, 0.5]$, $i = 1, 2, \dots, D$

Global minimum: $\mathbf{0}$ at $(0, 0, \dots, 0)$

IV. Implementation of the algorithms

The Cuckoo search algorithm, with each of the three above mentioned algorithms incorporated into it one by one to generate Lévy flight, is run 100 times. The population size is 25 and all the benchmark problems on which the algorithms are implemented are 15 dimensional unconstrained minimization problems. In Mantegna's algorithm the parameters are set as $\alpha = \frac{1}{2}$, $c = 1$. The simplified version algorithm uses parameter $\alpha = \frac{3}{2}$. McCulloch's algorithm takes the parameters $\alpha = 0.5$, $\beta = 0$ and $c = 1$. Also the pseudo code for the cuckoo search algorithm is given sequentially, but in order to take advantage of Matlab's vector capability, all new 25 solution vectors are generated at a time and then they get replaced one by one by better solutions.

V. Results obtained

With all the modifications *B* to *H* of the algorithm described above, Cuckoo Search algorithm is implemented on above mentioned benchmark problems *A* to *J*. The results obtained are analyzed in terms of the best and the worst solution, mean and the standard deviation of the optimum values obtained in 100 runs, the number of optimum values obtain within one

standard deviation interval, and the time of execution for 100 runs. The Count1 and Count2 variables in the table are showing, out of 100 runs how many optimum values are obtained within one and two standard deviation interval from the actual global minimum. The tabulated outputs are shown in the table 1 in appendix.

VI. Conclusion

From the outputs obtained, we see that McCulloch algorithm and simplified version of Mantegna's algorithm are more efficient than Mantegna's algorithm in terms of runtime. Further, addition of the Local Best term in the simplified version algorithm gives better results in many problems and comparable results in others with slight increase in the run time. However, replacing entire vector instead of some of its components does not reveal any significant improvement in the result, though it is preferable according to the base of the algorithm.

VII. Future work

As we have seen that the Cuckoo Search algorithm with simplified version of Mantegna's algorithm to generate Lévy flight is improved by adding the Local Best term. This improved version of CS can also be applied to constrained optimization problems to check its effect on the performance. At present, a fraction of the nests are replaced randomly. Instead, the poorer solutions can be prioritized for removal. Similarly, the probability of removal can also be varied and its appropriate value can be sought.

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Appendix

TABLE 1. Analysis of Outputs

A. Sphere function													
Algorithm	Best	Worst	Average	Std. dev.	Avg. No. of iterations	Count1	Count2	Elapsed time (S)					
B	3.2567e-006	9.9861e-006	8.7945e-006	1.1457e-006	30292	80	19	1879.80					
Solution vector corresponding to the best optimum value for Mantegna's Algorithm													
1.0004	0.9997	0.9999	0.9993	1.0003	0.9999	0.9998	1.0008	0.9998	0.9996	0.9990	0.9998	1.0001	0.9999
C	4.0631e-006	9.9896e-006	8.7270e-006	1.1517e-006	25054	75	23	59.01					
1.0002	1.0002	1.0005	1.0004	0.9989	1.0009	0.9998	1.0007	0.9999	0.9990	1.0001	1.0003	0.9998	0.9999
D	4.8812e-006	9.9891e-006	8.7563e-006	1.0407e-006	28903	72	27	51.53					
1.0012	0.9999	1.0004	0.9998	0.9995	1.0009	0.9993	1.0002	0.9997	1.0011	0.9998	1.0006	1.0001	0.9999
E	4.0289e-006	9.9999e-006	8.6139e-006	1.2774e-006	22709	75	24	99.21					
1.0002	1.0002	1.0005	0.9992	1.0013	1.0003	0.9998	1.0005	0.9995	0.9998	1.0004	1.0004	0.9995	1.0003

C	7.0603e-006	9.9921e-006	9.3225e-006	6.6777e-007	53039	83	15	119.74
-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000
-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000

D	6.0982e-006	9.9998e-006	9.3788e-006	6.3441e-007	63368	90	9	86.10
-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000
-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000

E	6.1740e-006	9.9913e-006	9.2191e-006	7.0416e-007	56561	80	18	189.73
-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000
-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000

F	6.5182e-006	9.9978e-006	9.3144e-006	7.4204e-007	67043	83	16	230.05
-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000
-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000

G	3.5900e-004	0.0237	0.0055	0.0040	250050	75	24	864.14
-0.5000	-0.5000	-0.5001	-0.4999	-0.5000	-0.4999	-0.5000	-0.5000	-0.5000
-0.5000	-0.5000	-0.5001	-0.4999	-0.5000	-0.4999	-0.5000	-0.5000	-0.5000

H	3.6564e-004	0.0177	0.0044	0.0030	250050	81	17	892.24
-0.5000	-0.4998	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000
-0.5000	-0.4998	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000	-0.5000

F. Levy function

B	5.2459e-006	9.9702e-006	8.6432e-006	1.1694e-006	49029	67	33	6137.60
0.9999	1.0012	0.9993	1.0001	1.0006	0.9988	0.9992	0.9994	0.9994
0.9999	1.0012	0.9993	1.0001	1.0006	0.9988	0.9992	0.9994	0.9994

C	4.2144e-006	9.9917e-006	8.8422e-006	1.2086e-006	52165	85	13	338.76
1.0000	0.9993	0.9988	0.9991	0.9996	1.0005	0.9990	0.9992	1.0005
1.0000	0.9993	0.9988	0.9991	0.9996	1.0005	0.9990	0.9992	1.0005

D	6.2420e-006	9.9940e-006	8.8758e-006	9.2807e-007	40731	68	32	228.21
0.9992	0.9996	1.0018	1.0005	0.9985	0.9991	0.9998	0.9996	0.9998
0.9992	0.9996	1.0018	1.0005	0.9985	0.9991	0.9998	0.9996	0.9998

E	3.6972e-006	9.9763e-006	8.9246e-006	1.1450e-006	49005	86	12	345.55
0.9997	1.0001	1.0005	1.0001	1.0003	0.9998	1.0013	0.9988	1.0004
0.9997	1.0001	1.0005	1.0001	1.0003	0.9998	1.0013	0.9988	1.0004

F	5.7284e-006	9.9887e-006	8.7916e-006	1.0038e-006	51325	69	30	368.60
0.9994	1.0007	0.9993	1.0005	0.9994	1.0004	0.9975	1.0004	1.0006
0.9994	1.0007	0.9993	1.0005	0.9994	1.0004	0.9975	1.0004	1.0006

G	7.2409e-006	1.3956e-004	1.7626e-005	2.0639e-005	125180	91	5	2142.80
1.0004	1.0004	1.0009	1.0014	0.9984	0.9996	0.9999	0.9990	1.0002
1.0004	1.0004	1.0009	1.0014	0.9984	0.9996	0.9999	0.9990	1.0002

H	7.0236e-006	0.0010	2.1247e-005	1.0299e-004	168845	99	0	1291.43
0.9988	0.9993	0.9989	1.0003	0.9987	1.0011	0.9995	0.9997	1.0006
0.9988	0.9993	0.9989	1.0003	0.9987	1.0011	0.9995	0.9997	1.0006

G. Generalized Schwfel 2.6 function

B	1.9095e-004	1.9100e-004	1.9099e-004	1.1584e-008	47138	75	25	2830.24
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	420.9688	420.9689	420.9688	420.9685	420.9690	420.9690	420.9688	420.9687	420.9690	420.9686	420.9686	420.9687
C	1.9095e-004	1.9100e-004	1.9099e-004	1.9099e-004	1.1858e-008	39452	75	25	130.09			
	420.9686	420.9689	420.9686	420.9689	420.9687	420.9689	420.9687	420.9686	420.9688	420.9688	420.9688	
D	1.9095e-004	1.9100e-004	1.9099e-004	9.8004e-009	47343	70	29	117.09				
	420.9686	420.9686	420.9687	420.9686	420.9684	420.9686	420.9689	420.9688	420.9688	420.9687	420.9688	420.9687
E	1.9095e-004	1.9099e-004	1.9098e-004	7.9203e-009	40190	82	17	162.97				
	420.9687	420.9687	420.9688	420.9690	420.9689	420.9690	420.9687	420.9688	420.9688	420.9685	420.9688	420.9687
F	1.9095e-004	1.9099e-004	1.9098e-004	8.5980e-009	49122	88	9	202.44				
	420.9687	420.9688	420.9686	420.9685	420.9689	420.9688	420.9687	420.9688	420.9689	420.9688	420.9687	420.9687
G	1.9098e-004	0.0031	3.4766e-004	3.6788e-004	242458	94	4	1059.23				
	420.9688	420.9690	420.9688	420.9688	420.9688	420.9690	420.9689	420.9690	420.9690	420.9687	420.9690	420.9686
H	1.9098e-004	5.4799e-004	2.3815e-004	7.7540e-005	245545	87	10	1048.99				
	420.9690	420.9687	420.9687	420.9687	420.9687	420.9688	420.9684	420.9692	420.9687	420.9684	420.9688	420.9689

H. Generalized Rozenbrock function

B	5.9126e-006	9.9910e-006	9.0904e-006	8.9282e-007	180592	82	17	10935.36						
	1.0000	1.0000	1.0000	0.9999	0.9999	0.9999	1.0000	1.0000	1.0000	0.9999	0.9999	0.9998	0.9997	0.9994
C	5.2451e-006	9.9989e-006	8.7796e-006	1.2255e-006	153918	80	20	416.28						
	1.0000	1.0001	1.0001	1.0001	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9996	
D	3.5767e-006	9.9861e-006	8.9595e-006	1.0825e-006	178861	87	11	342.38						
	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9997	0.9993	
E	6.4442e-006	9.9679e-006	9.1012e-006	8.6809e-007	178901	85	14	604.98						
	1.0000	1.0000	1.0000	1.0000	1.0000	1.0001	1.0001	1.0000	1.0000	1.0001	1.0001	1.0002	1.0004	
F	3.3758e-006	9.9981e-006	8.9790e-006	1.3726e-006	2786167	88	9	9695.60						
	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0001	1.0001	1.0001	1.0002	1.0004	
G	0.0049	4.2062	0.2952	0.5756	250050	96	2	915.23						
	0.9997	0.9996	0.9980	0.9990	1.0010	1.0004	1.0003	1.0006	1.0018	1.0007	0.9985	0.9959	0.9912	0.9823
H	0.0018	6.6209	0.6577	0.9572	250050	92	5	898.87						
	0.9992	1.0000	1.0010	0.9999	1.0008	1.0007	0.9996	0.9999	1.0001	1.0006	1.0007	1.0012	1.0029	1.0044

I. Rastrigin function

B	5.1106e-006	9.9937e-006	8.8557e-006	1.1609e-006	148996	85	14	17878.04						
	(0.0172	-0.1457	-0.0348	-0.0636	0.7672	0.5330	-0.2948	-0.2397	-0.2673	-0.1595	-0.6657	0.6431	0.7142	0.2578
C	5.7378e-006	9.9983e-006	8.9440e-006	1.0180e-006	117280	79	19	335.70						

	006	006	006	006		1.0e-004 *								
	(-0.2367	0.6540	-0.5494	-0.3404	-0.6498	-0.4619	0.1200	-0.4927	-0.0967	-0.3726	0.1325	-0.3121	-0.4535	0.1428
							0.7801)							
D	5.1870e-006	9.9959e-006	8.8865e-006				1.0213e-006	150460		79	20	308.76		
							1.0e-004 *							
	(0.5935	0.6347	0.2006	0.1777	-0.7579	-0.2038	-0.2997	-0.4182	0.0807	0.3540	-0.0561	0.5301	-0.0770	0.6941
							0.0572)							
E	4.6449e-006	9.9969e-006	8.9237e-006				9.3483e-007	111777		73	25	388.30		
							1.0e-004 *							
	(-0.4289	0.3301	0.0170	-0.5071	-0.2502	0.4892	-0.0266	-0.0260	0.25200.9068	0.2732	0.1134	-0.4025	-0.2850	
							0.5206)							
F	5.3737e-006	9.9841e-006	8.7024e-006				1.1478e-006	76599		71	29	273.38		
							1.0e-004 *							
	(0.6769	-0.6097	0.0239	-0.5833	-0.1260	0.1887	0.4944	0.1008	-0.38200.4067	-0.5938	0.1867	0.1583	0.6833	
							0.2029)							
G	7.9957e-006	2.7199	0.1361				0.5957	209400		95	0	798.18		
							1.0e-003 *							
	(-0.0002	0.0348	-0.0592	-0.0554	0.0334	0.0338	-0.0575	0.0279	-0.0530-0.0350	0.0419	0.1259	-0.0298	0.0550	
							0.0249)							
H	8.4836e-006	5.5275	1.3070				1.6926	249068		91	9	926.86		
							1.0e-003 *							
	(-0.0412	0.0288	-0.0448	-0.1092	0.1265	0.0195	-0.0147	-0.0286	-0.0054 -0.0458	-0.0712	0.0281	0.0224	0.0194	
							0.0006)							
J. Weierstrass function														
B	5.6438e-006	9.9953e-006	9.0794e-006				9.1828e-007	152255		83	15	13062.56		
							1.0e-010*							
	(-0.3072	0.1276	0.7386	0.3193	0.4202	0.1431	-0.1365	-0.1628	0.0228	-0.0438	-0.0686	-0.3037	-0.2694	0.9639
							-0.4146)							
C	5.0205e-006	9.9779e-006	8.8138e-006				1.1420e-006	176001		84	15	5320.60		
							1.0e-009 *							
	(-0.0442	-0.0088	0.1289	-0.0145	-0.0030	0.0144	0.0120	-0.0303	0.0051	-0.0424	0.0067	-0.0068	-0.0249	-0.0119
							0.0372)							
D	6.0728e-006	9.9969e-006	9.1135e-006				8.1877e-007	152575		72	26	4257.29		
							1.0e-010 *							
	(-0.4487	-0.3217	-0.2167	-0.1818	0.1428	0.0274	-0.1441	0.1908	0.3232	-0.3613	0.6083	0.8060	0.7243	0.3006
							0.0619)							
E	4.5747e-006	9.9979e-006	8.8024e-006				1.1522e-006	147530		81	16	4566.94		
							1.0e-010 *							
	(0.6775	-0.0590	-0.1896	-0.0588	0.1378	-0.3148	0.4213	-0.1647	-0.1570	-0.5015	0.7391	-0.1638	-0.1933	0.0000
							0.1660)							
F	5.5391e-006	9.9964e-006	9.1979e-006				9.0840e-007	165474		87	11	5090.04		
							1.0e-009 *							
	(0.0110	0.0271	0.0178	-0.0601	-0.0174	-0.0079	-0.1396	0.0202	-0.03680.0235	0.0043	-0.0246	0.0053	-0.0267	
							0.0002)							
G	0.0827	1.3395	0.3113				0.2484	250050		89	7	8400.94		
							1.0e-003 *							
	(0.0006	-0.0189	0.0000	-0.0000	0.0006	-0.0030	-0.0000	0.0050	-0.1524	0.0000	-0.0339	-0.0002	0.4575	-0.0000
							-0.0621)							
H	0.0697	1.0990	0.2130				0.1132	250050		92	7	7697.71		

(0.0081 -0.0009 -0.0017 -0.0004 0.1132 0.0001 1.0e-003 *
-0.0022 -0.1394 0.0150-0.0342 0.0357 0.0002 0.0018 -0.0003
0.0007)
